## IS IT A TRIANGLE? - SAMPLE RESPONSE

With your partner, use the provided GeoGebra activity to complete the table below. If a set of sides do not make a triangle, write "not a triangle" in the third column.
GeoGebra link: https://www.geogebra.org/m/tgwg6tnj.

| Number Sets | Is It a Triangle? <br> (Yes/No) | What Type of Triangle? <br> (Acute, Obtuse, Right) | $a+b$ | $<$ | $c$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $3,4,5$ | Yes | Right | 7 | $>$ | 5 |
| $1,2,3$ | No | Not a Triangle | 3 | $=$ | 3 |
| $6,5,10$ | Yes | Obtuse | Acute | 11 | $>$ |
| $12,16,18$ | Yes | No | Not a Triangle | 10 | $<$ |
| $7,3,12$ |  |  | 28 | $>$ | 18 |

How do we know if three line segments make a triangle?
When constructing a triangle, all three sides must meet the other at their endpoints. There cannot be any overlap or gaps.

What algebra can help us calculate this?

## Notation

$$
a+b>c
$$

How do we know what type of triangle a set of segments creates?
When constructing a triangle, you can use a protractor to determine the type of triangle you have.
What algebra can help us calculate this?

| Type of Triangle | Notation |
| :---: | :---: |
| Right | $a^{2}+b^{2}=c^{2}$ |
| Acute | $a^{2}+b^{2}>c^{2}$ |
| Obtuse | $a^{2}+b^{2}<c^{2}$ |

## IS IT A TRIANGLE? (TEACHER GUIDE)

Example Solutions for Lesson Slides

|  |  |
| :---: | :---: |
| Step 1: Ask yourself: Is it a triangle? $\begin{aligned} & a+b>c \\ & 5+12>13 \end{aligned}$ <br> This statement is true, therefore it's a triangle. | Step 1: Ask yourself: Is it a triangle? $\begin{aligned} & a+b>c \\ & 3+3>4 \end{aligned}$ <br> This statement is true, therefore it's a triangle. |
| Step 2: Classify the triangle. $a^{2}+b^{2} \square c^{2}$ <br> (Which symbol goes in the box? $=,\langle,>$ ) $\begin{aligned} & 5^{2}+12^{2} \square 13^{2} \\ & 25+144 \square 169 \\ & 169=169 \end{aligned}$ <br> Because the two sides of the expression equal each other, it is a right triangle. | Step 2: Classify the triangle. $a^{2}+b^{2} \square c^{2}$ <br> (Which symbol goes in the box? $=,\langle$,$\rangle )$ $3^{2}+3^{2} \square 4^{2}$ $\begin{aligned} & 9+9 \square 16 \\ & 18>16 \end{aligned}$ <br> Because the left side is larger than the right, it is an acute triangle. |
| Slide 27: 3, 4, 7 <br> Step 1: Ask yourself: Is it a triangle? $\begin{aligned} & a+b>c \\ & 3+4>7 \end{aligned}$ <br> This statement is true, therefore it's a triangle. <br> Step 2: Classify the triangle. $a^{2}+b^{2} \square c^{2}$ <br> (Which symbol goes in the box? $=,<,>$ ) $\begin{aligned} & \\ & 9+16 \square 49 \\ & 25<49 \end{aligned} \quad 3^{2}+4^{2} \square 7^{2}$ <br> Because the left side is less than the right, it is an obtuse triangle. |  |

