

GUIDED NOTES: BOUNCE WIGGLE CROSS

Directions:

1. Use the following window values:
 - i. $[x \text{ min}, x \text{ max}] = [-3, 4]$ $[y \text{ min}, y \text{ max}] = [-100, 100]$ $\text{yscl} = 0$
2. Graph each $f(x)$ on your calculator.
3. Sketch the graph on the chart. Do not worry about the scale. We are only interested in the end-behaviors and the behavior at the x -intercepts.
4. Fill in the remaining columns of the chart based on the information you see on your graph.

After completing the table:

1. Look at each root where the graph of $f(x)$ "crossed" the x -axis. What was the power of the corresponding factor?
2. Look at each root where the graph of $f(x)$ wiggled at the x -axis. What do you notice about the power of the corresponding factor?
3. Look at each root where the graph of the $f(x)$ is tangent or bounced at the x -axis. What do you notice about the power of the corresponding factor?

4. If $f(x)$ has the highest-powered term ax^n , describe the end behavior of the $f(x)$ in each of the following situations:

$a > 0$, n is even: _____

$a < 0$, n is even: _____

$a > 0$, n is odd: _____

$a < 0$, n is odd: _____

EXTENSION: BOUNCE WIGGLE CROSS

Calculus Connection:

A particle starts at time $t = 0$ and moves along the x -axis so that its position at any time $t \geq 0$ is given by:

$$x(t) = (t - 1)^3(2t - 3).$$

For what values of t is the velocity of the particle less than zero?

(Hint: factor the algebraic expression, then sketch a quick sketch using the x -intercepts and the behavior of the exponents to find where the function is < 0 .)

$$V(t) = 2(t - 1)^3 + 3(t - 1)^2(2t - 3)$$